Ranges of moisture-source temperature estimated from Antarctic ice cores stable isotope records over glacial–interglacial cycles

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Abstract. A single isotope ratio (δD or δ18O) of water is widely used as an air-temperature proxy in Antarctic ice core records. These isotope ratios, however, do not solely depend on air-temperature but also on the extent of distillation of heavy isotopes out of atmospheric water vapor from an oceanic moisture source to a precipitation site. The temperature changes at the oceanic moisture source (ΔT\text{source}) and at the precipitation site (ΔT\text{site}) can be retrieved by using deuterium-excess (d) data. A new d record from Dome Fuji, Antarctica spanning the past 360 000 yr is presented and compared with records from Vostok and EPICA Dome C ice cores. In previous studies, to retrieve ΔT\text{source} and ΔT\text{site} information, different linear regression equations were proposed using theoretical isotope distillation models. A major source of uncertainty lies in the coefficient of regression, β\text{site} which is related to the sensitivity of d to ΔT\text{site}. We show that different ranges of temperature and selections of isotopic model outputs may increase the value of β\text{site} by more than a factor of two. To explore the impacts of this coefficient on reconstructed temperatures, we apply for the first time the exact same methodology to the isotope records from the three Antarctica ice cores. We show that uncertainties in the β\text{site} coefficient strongly affect (i) the glacial–interglacial magnitude of ΔT\text{source}; (ii) the imprint of obliquity in ΔT\text{source} and in the site-source temperature gradient. By contrast, we highlight the robustness of ΔT\text{site} reconstruction using water isotopes records.

1 Introduction

Climate records preserved in Antarctic ice cores provide important clues for the climate history over the several hundred thousand years. Among many deep ice cores from Antarctica, Vostok (Petit et al., 1999), EPICA Dome C (hereafter EDC) (EPICA Community Members, 2004; Jouzel et al., 2007) and Dome Fuji cores (hereafter DF) (Watanabe et al., 2003) have provided climate and environmental information covering multiple glacial–interglacial cycles. δD and δ18O of water are widely used as proxies for air-temperature, albeit with uncertainties in temperature reconstructions arising from possible changes in precipitation intermittency (Steig et al., 1994; Sime et al., 2009; Laepple et al., 2011), ice sheet elevation (Masson-Delmotte et al., 2011), or evaporation conditions (Boyle, 1997).

The latter source of uncertainty can be explored using a second-order isotopic information available through deuterium-excess (d = δD − 8 × δ18O) (Dansgaard, 1964). The d parameter mainly gives access to processes affected by kinetic fractionation and has been used as a tracer of evaporation conditions such as ocean surface temperature and relative humidity in moisture source ocean (Merlivat and Jouzel, 1979). The d value of modern atmospheric vapor above the Southern Ocean shows a clear dependency on sea surface temperature and relative humidity at the moisture source (Uemura et al., 2008). The initial information is then modified by subsequent meteorological processes.
(e.g. precipitation, snow formation, and cloud microphysics). The Antarctic precipitation $d$ value is therefore also affected by kinetic fractionation during the snow formation, whose importance is expressed by a supersaturation function (Jouzel and Merlivat, 1984; Risi et al., 2010; Winkler et al., 2012), and by equilibrium distillation at very cold temperatures as well as the amount of rainout from the source to sink.

At first order, past variations of $\delta D$ and $d$ in ice cores are assumed to mostly depend on polar temperature ($\Delta T_{\text{site}}$), moisture source temperature ($\Delta T_{\text{source}}$), and ocean isotopic composition ($\delta^{18}D_{\text{sw}}$ and $\delta^{18}O_{\text{sw}}$). Source and site climatic information can therefore be extracted from ice core $\delta D$ and $d$ records, using a linear regression model based on the Rayleigh distillation isotopic model and/or more sophisticated models (Vimeux et al., 2001; Cuffey and Vimeux, 2001; Stenni et al., 2001, 2010). This dual isotope approach allows corrections to site temperature estimates for moisture source effects. Such site and source temperature inversions have been conducted using different methodologies (e.g. different adjustments of the linear regression coefficients) for Vostok (Cuffey and Vimeux, 2001; Vimeux et al., 2002), EDC (Stenni et al., 2001, 2003, 2010), and EPICA Dronning Maud Land (EDML) (Stenni et al., 2010) ice cores. These studies reveal the importance of obliquity in modulating Vostok (Cuffey and Vimeux, 2001; Vimeux et al., 2002), EDC (Stenni et al., 2001, 2003, 2010), and EPICA Dronning Maud Land (EDML) (Stenni et al., 2010) ice cores. These studies reveal the importance of obliquity in modulating Vostok source temperature (Vimeux et al., 2002). It has also been shown that source correction enhances the correlation between Vostok $\Delta T_{\text{site}}$ and atmospheric CO$_2$ during glacial inceptions (Cuffey and Vimeux, 2001), and that glacial millennial Antarctic Isotopic Maxima largely reflect changes in site temperature (Stenni et al., 2003). However, there are no common methodologies and are still significant uncertainties about reconstructing site and source temperatures.

Indeed, it is not possible to assess the full range of unknown source parameters (source temperature, relative humidity, wind speed) with only two isotope measurements ($\delta D$ and $\delta^{18}O$) (Stenni et al., 2010). To overcome this problem, different approaches have been developed to account for the ocean isotopic changes and relative humidity effect (Vimeux et al., 2001; Cuffey and Vimeux, 2001; Stenni et al., 2001, 2003). The largest difference between these studies is associated with the coefficient describing the sensitivity of $d$ to $\Delta T_{\text{site}}$, hereafter $\beta_{\text{site}} (=-\partial d/\partial T_{\text{site}})$, for which different studies have used values ranging from $\sim$0.5 (Cuffey and Vimeux, 2001; Stenni et al., 2001) to 1.2 (Salamatin et al., 2004). In this manuscript, we review the causes for differences in $\beta_{\text{site}}$ and the subsequent impacts on $\Delta T_{\text{source}}$ and $\Delta T_{\text{site}}$ reconstructions for the three central East Antarctic ice cores using published isotope profiles from Vostok and EDC, and a new deuterium excess record from DF.

This manuscript is organized as follows: ice-core data and isotope modeling are described in Sect. 2, while causes for the $\beta_{\text{site}}$ differences and their impacts on $\Delta T_{\text{source}}$ and $\Delta T_{\text{site}}$ are discussed in Sect. 3 and site and source reconstructions in Sect. 4.

### 2 Isotope data and modeling

#### 2.1 Ice core isotopic data

We used the three deep ice cores drilled in East Antarctica, DF, Vostok and EDC. The DF data were extended and revised in this paper (Fig. 1). Two ice cores were drilled at the DF station ($77^\circ 19^\prime S, 39^\circ 42^\prime E$, elevation 3810 m). The first 2503 m-depth core (DF1) was drilled in 1996, and revealed the $\delta^{18}O$ and $\delta D$ records back to $\sim$340 kyr BP (thousands of years before present) (Watanabe et al., 2003; Uemura et al., 2004). A second core (Dome Fuji 2nd, DF2) reached near bedrock in 2007 at the depth of 3035.2 m (Motoyama, 2010a). Here, we present $\delta D$ and $d$ records from the $\sim$130 m-length section of the DF2 core at 10 cm-length sampling from every 50 cm ($n = 265$). The $\delta D$ data from the overlapping section (2400–2500 m) of DF 1 and DF2 shows remarkable similarity (Fig. 2).

The DF isotope ratios were measured using an equilibration method (Uemura et al., 2007) at National Institute of Polar Research, Japan. Routine measurements (2006 to 2008) of a reference water sample show that reproducibilities ($\sigma$) of this water are 0.3‰ for $\delta D$, 0.04‰ for $\delta^{18}O$, and 0.4‰ for $d$. Duplicate analyses for 119 ice core samples confirm these estimates. In order to obtain the revised $d$ record for the entire DF core, a new data set was made by (1) subtracting artificial isotope offsets from the DF1 record (see below) and (2) replacing the DF1 data by DF2 data for the overlapping part (2400–2503 m).

First, there are offsets between DF1 and DF2 ($\delta_{\text{DF1}} - \delta_{\text{DF2}} = 0.8$‰ for $\delta D$, and 0.24‰ for $\delta^{18}O$). In order to
assess the potential causes of this offset, we re-cut and measured the archived DF1 ice (~60 samples). The re-cut DF1 data are consistent with that of measured DF2 data (i.e. no offset), but lower than that of the old DF1 data. This result suggests that only the “old DF1” data are isotopically enriched slightly than both “re-cut DF1” and “DF2” data due to some artifacts. This is probably caused by problems in the storage of the DF1 samples preserved in glass vials as liquid. Based on our experiment, isotopic enrichment during long term storage may explain half (~0.1‰) for 818O of the observed offset between DF1 and DF2. So far, we cannot explain the full magnitude of the offset between DF1 and DF2. The offsets of δ values were subtracted from the published data (Watanabe et al., 2003; Uemura et al., 2004). We should note that the offset discussed here is systematic, small compared with glacial–interglacial variations (1.3% of full amplitude), and does not affect magnitudes of events. Therefore, the correction applied here does not influence the conclusions of earlier studies.

Second, an enlarged view of the records clearly shows that the d data are less noisy for DF2 than for DF1, suggesting that the precision of the new data is improved by replicate measurements of many (~30%) samples (Fig. 2). Thus, we replaced DF1 record by DF2 for the overlapping period.

For Vostok (78°30′S, 106°54′E, elevation 3488 m), the d data span the past ~420 kyr BP (Vimeux et al., 2001). We restricted the ice core comparison over the past 250 kyr because the deepest part of the data is likely affected by changes in ice origin due to ice flow (Vimeux et al., 2001). For the EDC core (75°06′S, 123°23′E, elevation 3233 m), we used the recently published record spanning over the last 140 kyr BP (Stenni et al., 2010). Another d record from EDML (75°00′S, 00°09′E, elevation 2892 m) is also available for the same period but was not considered here because of uncertainties in elevation/ice origin impact (Stenni et al., 2010).

Precisions of 818O and δD measurements of both the Vostok and EDC cores are 0.05‰ and 0.5‰, respectively, (Vimeux et al., 2001; Stenni et al., 2010) with a final precision of 0.6‰ on d. Therefore, the analytical accuracies of the 3 ice cores isotopic records are similar. The temporal resolution, which is estimated a using cutting scale combined with a depth-age scale, however, differs between records. The average temporal resolution of the DF data is ~270 yr, except for the ~70 yr resolution during the Holocene. At Vostok, the average temporal resolution is ~220 yr for our period of interest (Vimeux et al., 2001). The EDC core shows the highest temporal resolution; ~18 yr for the Holocene, ~50 yr for MIS2 and ~42 yr for MIS5.5 (Stenni et al., 2010). We place the ice core isotopic records on a common age scale in order to be able to make a comparison. As shown in Fig. 3, significant differences (up to ~5 kyr) exist between the glaciological age scales established for Vostok (GT4 age-scale by Petit et al., 1999) and EDC (EDC3 age-scale by Parrenin et al., 2007) and the O2/N2 orbital age scale for DF (Kawamura et al., 2007). The age-scale difference between Vostok and DF is ~1 kyr before 80 kyr BP, and increased up to ~5 kyr around 120 kyr BP, and between EDC and DF is ~1 kyr before 80 kyr BP, and increased up to ~4 kyr for the older part. Here, we use the DF age scale as a target and synchronized the Vostok, EDC and our new stacked DF record using visual δD matching (Fig. 3). We used 21 tie points for DF-Vostok fitting, and nine tie points for DF-EDC fitting. For the calculation of ΔTs and ΔTsource, all the data were re-sampled with 200-yr resolution, which is under-sampling for EDC data, and slightly over-sampling for Vostok and DF data.

Note that this temporal resolution is the result of the sampling strategy, combined with the depth-age scale, resulting from changes in accumulation and thinning. The ability to resolve past high frequency climatic variations also depends on isotopic smoothing caused by diffusion in firm and ice. The diffusion length at EDC was estimated at 8 cm for MIS11 (Pol et al., 2011), deeper than for our studied periods. For example, the sampling length of about 165 cm

Fig. 2. δD and deuterium-excess records from the DF ice cores. (a) δD and d records from DF1 (black lines) and DF2 (blue lines) cores. (b) Enlarged view of the d records during the overlapping period. Here, δ = Rample/RVSMOW − 1, and Rample and RVSMOW are the isotope ratios (D/H and 18O/16O) of sample and VSMOW, respectively.

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at EDC (at \( \sim 1460 \) m depth, \( \sim 108 \) kyr BP) corresponding to 200 yr resolution.

2.2 Raw \( d \)-excess and \( \delta D \) data

The raw \( d \) records from the DF, Vostok, and EDC ice cores show common low frequency variability (\( \sim 40 \) kyr) (Fig. 2). There are periods of pronounced \( d \) minima in the older sections (200–250 kyr BP) at DF and Vostok, and both the records show similar variations. A difference can be found during the glacial terminations. From 20 to 10 kyr BP (Termination I), the onset of \( d \) increases in DF and Vostok appears to lag that of EDC. From 140 kyr to 130 kyr BP (Termination II), a similar lag is observed (Fig. 3). It is difficult to interpret the raw \( d \) record because it is an empirically defined second-order parameter. In fact, a different definition of \( d \) parameter can produce different glacial interglacial variations (see Sect. 3 and Appendix A). Climatic interpretation of \( d \) will be discussed after inferring \( \Delta T_{\text{source}} \) from isotopic data (Sect. 4).

2.3 Isotope inversion method

In order to retrieve the climatic information from the isotope ratios, we need to evaluate several coefficients using an isotope model. Sensitivities of \( \delta D \) and \( d \) to \( \Delta T_{\text{source}} \), \( \Delta T_{\text{site}} \), relative humidity (RH), and ocean isotopic composition (\( \delta^{18}O_{\text{sw}} \)) were estimated using a mixed cloud isotopic model (MCIM) developed by Ciais and Jouzel (1994).

We used the linear inversion method that is similar to the method used for Vostok (Cuffey and Vimeux, 2001) and EDC records (Stenni et al., 2001, 2003, 2010; Masson-Delmotte et al., 2004).

There are several differences among the inversion methods used for various ice cores. First, the coefficients for the correction for \( \delta^{18}O_{\text{sw}} \) were used as fixed parameters in several studies (Vimeux et al., 2001, 2002; Cuffey and Vimeux, 2001; Stenni et al., 2001). This coefficient is calculated as a function of the isotopic composition of the ice (Vimeux et al., 2001; Jouzel et al., 2003; Kavanaugh and Cuffey, 2003), as follows:

\[
\delta^{18} O_{\text{corr}} = \delta^{18} O_{\text{ice}} - \delta^{18} O_{\text{sw}} \frac{(1 + \delta^{18} O_{\text{ice}})}{(1 + \delta^{18} O_{\text{sw}})} \tag{1}
\]

\[
\delta D_{\text{corr}} = \delta D_{\text{ice}} - \delta D_{\text{sw}} \frac{(1 + \delta D_{\text{ice}})}{(1 + \delta D_{\text{sw}})} \tag{2}
\]

Here, \( \delta^{18} O_{\text{corr}} \) and \( \delta D_{\text{corr}} \) are the isotope ratios of the ice (\( \delta^{18} O_{\text{ice}} \) and \( \delta D_{\text{ice}} \)) corrected for ocean isotope changes (\( \delta^{18} O_{\text{sw}} \) and \( \delta D_{\text{sw}} \)). An estimate of the global ice volume component of sea-water \( \delta^{18} O \) (Bintanja and Wal, 2008) was used for the \( \delta^{18} O_{\text{sw}} \) record. The \( \delta D_{\text{sw}} \) is calculated on the assumption that \( \delta D_{\text{sw}} = 8 \times \delta^{18} O_{\text{sw}} \). Thus, the \( d \) value corrected for the ocean isotope effect (\( d_{\text{corr}} \)) is obtained by \( d_{\text{corr}} = \delta D_{\text{corr}} - 8 \delta^{18} O_{\text{corr}} \). Following recent studies (e.g. Stenni et al., 2010), we apply this correction before conducting the multiple linear regression.
Second, $\delta D$ and $d$ in polar precipitation preserve source effects and therefore depend on climatic parameters affecting evaporation kinetics, including $\Delta T_{\text{source}}$ but also relative humidity (RH) and wind-speed regimes (Merlivat and Jouzel, 1979; Petit et al., 1991). For Vostok, the RH effect was explicitly included in the $\Delta T_{\text{source}}$ by using a linear relationship identified in Atmospheric General Circulation Models ($\Delta h \sim -0.4 \Delta T_{\text{source}}$) (Vimeux et al., 2001; Cuffey and Vimeux, 2001). For EDC, the RH effect was not included, restricting the analyses of source effects to $\Delta T_{\text{source}}$ only (Stenni et al., 2001). Here, we adopted the latter approach for the sake of simplicity. Thus, the results of multiple linear regressions can be expressed as

\[
\Delta \delta D_{\text{corr}} = \gamma_{\text{site}} \Delta T_{\text{site}} - \gamma_{\text{source}} \Delta T_{\text{source}}
\]

\[
\Delta d_{\text{corr}} = -\beta_{\text{site}} \Delta T_{\text{site}} + \beta_{\text{source}} \Delta T_{\text{source}}
\]

All the $\gamma$ and $\beta$ coefficients are positive numbers expressed in $\%$ per K. The $\Delta$ represents deviations from the present reference values (in this study “present” is defined as the averaged value of the past 2 kyr). The $\Delta T_{\text{site}}$, mean annual temperature at ground level, is calculated from the mean annual temperature of condensation ($\Delta T_c$) by assuming a constant relation ($\Delta T_c = 0.67 \Delta T_{\text{site}}$) (Jouzel and Merlivat, 1984). This is an approximation as the Antarctic inversion strength varies spatially and in time, and with changing weather conditions. Recently, a detailed analysis of the half century long meteorological observations at Vostok allowed to estimate changes in condensation temperature and confirmed the validity of this approach (Ekaykin, 2003).

Finally, kinetic isotope fractionation occurs during ice crystal growth because of super-saturation over ice, and this is parameterized using a linear function of temperature tuned to reproduce the spatial $d$ vs. $\delta$ distribution in Antarctica (Petit et al., 1991). We used a linear function ($Si = 1.020 - 0.003T$) which best reproduces the present-day surface snow $d$ vs. $\delta D$ distribution from various parts of Antarctica (Masson-Delmotte et al., 2008), and from Japanese–Swedish IPY 2007/2008 traverse covering Syowa-Dome F route (black dotted line) (Fukui et al., 2010). Simulated curves are shown as blue solid line (Case 1), blue line (Case 2) and blue dotted line (Case 3). Each case corresponds to different super saturation functions shown in Table 3. Dots represent ice-core data of DF over the past 360 kyr (red), Vostok over the past 250 kyr (blue), and EDC over the past 140 kyr (green). Here, $\delta D$ and $d$ are corrected for $\delta^{18}O_{\text{sw}}$, see text for detail.

### 2.4 Present-day isotope tuning

The first step for estimating the sensitivity coefficients is to fit the model output to the present-day snow isotopic distribution (Fig. 4). An important problem of this tuning is the difficulty to simulate present-day snow isotope ratios by using the MCIM. At the DF site, the present-day (past 2 kyr average ±1σ) isotope ratios are $\delta^{18}O = -55.09 \pm 0.16 \%_e$, $\delta D = -426.3 \pm 1.4 \%_e$, and $d = 14.4 \pm 0.3 \%_e$. With our MCIM tuning, these isotope ratios can only be reached with a very cold site temperature (i.e. annual mean air temperature at the surface snow), $-61.0^\circ C$, which is significantly lower than the 10 m-depth temperature of $-57.7^\circ C$ (Motoyama et al., 2005) and 1-yr observations at 4 m-height of $-54.8^\circ C$ (Fujita and Abe, 2006).

The difficulties in simulating present-day $\delta$ values also reflect the difference between annual mean temperature and precipitation weighted temperature (e.g. Masson-Delmotte et al., 2011), and/or differences in prescribed surface airpressures. In fact, the air pressure at DF is the lowest among the coring sites due to its high elevation (3810 m a.s.l.), compared with the Vostok (3488 m a.s.l.) and EDC (3233 m a.s.l.). Lower air-pressure results in smaller distillation in the model, and thus produces higher simulated $\delta$ values.

We therefore have two options. Either we use a “realistic” DF temperature and perform regressions in an isotope range that is not sufficiently depleted when compared to the data; or we use colder than observed temperatures (and associated fractionation coefficients) to perform the regressions on the isotopic model results. Here, we explore the impacts of the second option of an “isotope fitted” procedure. We note that, as calibration targets, averaged isotope ratios are more reliable than Antarctic annual-mean temperature data due to the short instrumental records for instance at DF.
In principle, $\beta_{\text{site}}$ value of 0.6 of “Temperature fitted 2” is comparable to the values (0.5) used in previous ice core reconstructions. Thus, we conclude that most of the discrepancy found between previous studies can be explained by the choices of different methodologies: whether the model is tuned to reproduce the observed ice core isotope ratios (Salamatin et al., 2004), or is driven by realistic air-temperatures (Cuffey and Vimeux, 2001; Stenni et al., 2001). Our approach accounting for large slopes at cold temperatures allows us to explore this source of uncertainty on reconstructing site and source temperatures.

We tested the $\beta_{\text{site}}$ sensitivity to different supersaturation functions, corresponding to the upper and lower bounds compatible with present day data (Table 3, Fig. 4). These simulations were conducted with super saturation function (Si), 1.020–0.0025 $T$ and 1.020–0.0035 $T$, respectively. In such a sensitivity test, it is difficult to reproduce correctly the present-day surface snow isotopic values, and we cannot select data for regression analysis based on ice core data (see Sect. 3.2). Consequently, we performed regression analysis by varying $\Delta T_{\text{site}}$ and $\Delta T_{\text{source}}$ by $\pm 2^\circ C$. The results show that the impact of different super-saturation functions on the value of $\beta_{\text{site}}$ is about 20%, and that of the other parameters is marginal (Table 3). Therefore, the super saturation affects the $\beta_{\text{site}}$ parameters, but the impact is small compared with its sensitivity to different site and source temperatures conditions (Table 2).
Table 1. Comparison of the temperature inversion coefficients.

<table>
<thead>
<tr>
<th>Site</th>
<th>(\beta_{\text{site}})</th>
<th>(\beta_{\text{source}})</th>
<th>(\gamma_{\text{site}})</th>
<th>(\gamma_{\text{source}})</th>
<th>(\gamma_{\text{sw}})</th>
<th>Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>DF</td>
<td>1.3</td>
<td>1.6</td>
<td>7.7</td>
<td>3.2</td>
<td>–</td>
<td>This study</td>
</tr>
<tr>
<td>Vostok(^a)</td>
<td>0.5</td>
<td>1.3</td>
<td>2.8</td>
<td>7.1</td>
<td>3.7</td>
<td>4.8</td>
</tr>
<tr>
<td>Vostok(^b)</td>
<td>0.9, 1.2</td>
<td>1.1, 1.2</td>
<td>3.0, 2.9</td>
<td>6.8, 6.9</td>
<td>2.8, 3.6</td>
<td>4.5, 4.7</td>
</tr>
<tr>
<td>Vostok(^{a,b,c})</td>
<td>1.0</td>
<td>1.4</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
</tr>
<tr>
<td>Vostok(^c)</td>
<td>1.1</td>
<td>1.5</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>–</td>
</tr>
<tr>
<td>Vostok</td>
<td>1.4</td>
<td>1.6</td>
<td>–</td>
<td>7.7</td>
<td>3.1</td>
<td>–</td>
</tr>
<tr>
<td>EDC(^a)</td>
<td>0.5</td>
<td>1.3</td>
<td>2.6</td>
<td>7.6</td>
<td>3.5</td>
<td>5.0</td>
</tr>
<tr>
<td>EDC</td>
<td>0.5</td>
<td>1.3</td>
<td>–</td>
<td>7.6</td>
<td>3.6</td>
<td>–</td>
</tr>
<tr>
<td>EDC</td>
<td>1.2</td>
<td>1.5</td>
<td>–</td>
<td>7.8</td>
<td>3.4</td>
<td>–</td>
</tr>
<tr>
<td>East Antarctica(^a,b,c)</td>
<td>1.29 to 2.04</td>
<td>1.31 to 1.5</td>
<td>3</td>
<td>–</td>
<td>–</td>
<td>–</td>
</tr>
</tbody>
</table>

\(^a\) Corrections for ocean isotope changes were estimated using \(\beta_{\text{sw}}\) and \(\gamma_{\text{sw}}\): \(\Delta T = \beta_{\text{site}} \Delta T_{\text{site}} + \beta_{\text{source}} \Delta T_{\text{source}} - \beta_{\text{sw}} \Delta \delta^{18}O_{\text{sw}}\), and \(\Delta D = \gamma_{\text{site}} \Delta T_{\text{site}} - \gamma_{\text{source}} \Delta T_{\text{source}} + \gamma_{\text{sw}} \delta D_{\text{sw}}\). See the Sect. 2.3 for detail.\(^b\) Condensation temperature at precipitation deposition site \((\Delta T_{\text{sw}})\) used in original paper was converted to temperature at ground level \((\Delta T_{\text{cor}})\) using a linear relation \(\Delta T = 0.67 \Delta T_{\text{site}}\) (Jouzel and Merlivat, 1984). Thus, the \(dT_{\text{cor}}\) slopes (1.7 and 1.4 for 2 different trajectories) correspond to the values of 1.2 and 0.9 for \(\beta_{\text{sw}}\).\(^c\) Variations of relative humidity was estimated as an independent parameter.

Table 2. Test of \(\beta_{\text{site}}\) sensitivity to the source and site temperatures.

<table>
<thead>
<tr>
<th>Tuning strategy</th>
<th>Simulated DF isotope ratio (%)</th>
<th>Temperature (°C)</th>
<th>Sensitivity coefficient (%°C)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>δD</td>
<td>δ(^{18})O</td>
<td>(d)</td>
</tr>
<tr>
<td>Isotope fitted</td>
<td>–422.7</td>
<td>–54.6</td>
<td>14.5</td>
</tr>
<tr>
<td>Temperature fitted 1</td>
<td>–377.1</td>
<td>–48.2</td>
<td>8.5</td>
</tr>
<tr>
<td>Temperature fitted 2</td>
<td>–351.1</td>
<td>–43.9</td>
<td>–0.2</td>
</tr>
</tbody>
</table>

3.2 Data selection for regressions

Another methodology that affects the \(\beta_{\text{site}}\) value is the data selection criteria used for establishing the multiple linear regressions coefficients. In previous studies, the regression analyses were performed on the simulated \(\delta\) values in response to a wide range of randomly changed climate conditions \((\Delta T_{\text{site}}, \Delta T_{\text{source}})\) (e.g. Masson-Delmotte et al., 2004). The large range of results obtained for DF with this approach is illustrated in Fig. 5 as open circles.

In contrast, we propose to restrict the range of site and source conditions for which the modeled isotopic results are consistent with the glacial–interglacial ice core data. Note that our model results account for sea water isotopic composition corrections; this is a marginal source of uncertainty in the model-data comparison. We therefore selected a subset of the modelled isotope values (and corresponding \(\Delta T_{\text{site}}\) and \(\Delta T_{\text{source}}\)) displayed as black circles in Fig. 5, and performed the multiple linear regression analysis on this dataset. We illustrate in Fig. 5 the importance of this data selection for the \(d\)-\(\delta D\) slopes, which increase with isotopic depletion and temperature ranges. Generally, excluding higher \(\delta D\) data results in larger \(d\)-\(\delta D\) slope and thus larger \(\beta_{\text{site}}\) coefficient. Our approach results in a larger \(\beta_{\text{site}}\) coefficient compared to the previous approaches.

These results suggest that our methodology, using the MCIM model with deliberately cold conditions and selected data, should be seen as an upper end approach for the \(\beta_{\text{site}}\) coefficient, compared to previous approaches which did not sufficiently account for the large slope at cold temperatures.

3.3 Different sensitivity coefficients

The isotope inversion was performed to retrieve the \(\Delta T_{\text{site}}\) and \(\Delta T_{\text{source}}\) information using the method described above (\(\text{SI} = 1.020 - 0.003T\)), and present \(T_{\text{site}}\) and simulated \(\delta\) values are shown as isotope fitted in Table 1). The linear relations obtained for the DF ice core are

\[ \Delta \delta D_{\text{corr}} = 7.7 \Delta T_{\text{site}} - 3.2 \Delta T_{\text{source}} \]
\[ (R^2 = 0.999, n = 14, p < 0.001) \] (5)

\[ \Delta d_{\text{corr}} = -1.3 \Delta T_{\text{site}} + 1.6 \Delta T_{\text{source}} \]
\[ (R^2 = 0.989, n = 14, p < 0.001) \] (6)

The linear correlations are strong, thus the statistical uncertainty of each coefficient due to multiple regression analysis is very small (0.03 to 0.05). The uncertainty caused by the data selection for the regression analysis (Sect. 3.2) is also small. In fact, if we remove several (1 to 5) points located around the “corner” of data subset (Fig. 5), the uncertainties

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The new coefficients obtained in this study (Eqs. 5 and 6) were applied to the DF ice core data to estimate past variations in $\Delta T_{\text{source}}$ and $\Delta T_{\text{site}}$ (Fig. 6). The new $\Delta T_{\text{source}}$ ranges from $-5.9^\circ\text{C}$ to $2.9^\circ\text{C}$ over the past 360 kyr. The record shows maxima of $\Delta T_{\text{source}}$ occurring during Marine Isotope Stage (MIS) 5e and MIS 9e with values respectively 2.6 $\pm$ 0.3 $^\circ\text{C}$ and 2.9 $\pm$ 0.3 $^\circ\text{C}$ higher than present. A glacial minimum at 19 kyr BP is $-5.9^\circ\text{C}$. Here, temperatures are based on the average and $\pm1$ kyr duration around the maximum or minimum point. This $\Delta T_{\text{source}}$ reconstruction remains high when $\Delta T_{\text{site}}$ and $\Delta T_{\text{low}}$ drop during glacial inceptions, linked with high $d$ values during the onset of glaciations. The DF $\Delta T_{\text{site}}$ derived from the new coefficients ranges

![Fig. 6. Different $\Delta T_{\text{source}}$ and $\Delta T_{\text{site}}$ of DF and a stacked SST records. (a) Black line represents the $\Delta T_{\text{source}}$ record of DF core based on the coefficients ($\beta_{\text{site}} = 1.3$) obtained by isotope-fitting (this study). Blue line represents the $\Delta T_{\text{source}}$ record of DF core based on the coefficients ($\beta_{\text{site}} = 0.5$) used for Vostok reconstruction (temperature-fitting) (Cuffey and Vimeux, 2001; Vimeux et al., 2002). Numbers indicate Marine Isotope Stages. (b) Black line is the $\Delta T_{\text{source}}$ of DF core, same as (a), but with a stacked southern SST record of ocean sediments (Barrows et al., 2007) (red line). (c) The $\Delta T_{\text{site}}$ record based on the coefficients of this study (black line), $\Delta T_{\text{low}}$ (blue line), and previous $\Delta T_{\text{site}}$ reconstruction of DF core (temperature-fitting) (Kawamura et al., 2007).]

### Table 3. Test of $\beta_{\text{site}}$ sensitivity to the super saturation function.

<table>
<thead>
<tr>
<th>Super saturation function ($S_i$)</th>
<th>Simulated DF isotope ratio (‰)</th>
<th>Temperature (°C)</th>
<th>Coefficient (%/°C)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$\delta D$ $\delta^{18}\text{O}$ $d$</td>
<td>Site</td>
<td>Source</td>
</tr>
<tr>
<td>1.020–0.0030T (case 1)</td>
<td>-422.7 -54.6 14.5</td>
<td>-61.0 18.0</td>
<td>1.3 1.6 7.7 3.2</td>
</tr>
<tr>
<td>1.020–0.0025T (case 2)</td>
<td>-403.6 -52.2 13.9</td>
<td>-58.0 18.0</td>
<td>1.2 1.4 7.7 3.3</td>
</tr>
<tr>
<td>1.020–0.0035T (case 3)</td>
<td>-441.3 -57.0 14.3</td>
<td>-64.0 18.0</td>
<td>1.1 1.6 7.5 3.0</td>
</tr>
</tbody>
</table>
from $-7.8 \pm 0.2 ^\circ C$ to $4.8 \pm 0.5 ^\circ C$ over the past 360 kyr. Maximum $\Delta T_{\text{site}}$ occur during MIS 9e, with temperature $4.8 \pm 0.5 ^\circ C$ warmer than that of present-day average.

In order to show the importance of the value of $\beta_{\text{site}}$, other $\Delta T_{\text{source}}$ and $\Delta T_{\text{site}}$ records which were obtained using the smaller values of $\beta_{\text{site}}$ (0.5) and other coefficients used in Cuffey and Vimeux (2001) (Table 1) are shown in Fig. 6a. For clarity, we labeled this $\Delta T_{\text{source}}$ and $\Delta T_{\text{site}}$ records based on the smaller $\beta_{\text{site}}$ coefficient as $\Delta T_{\text{low source}}$ and $\Delta T_{\text{low site}}$, respectively. Two major differences are identified for the source temperature records. First, the glacial–interglacial amplitude of the new $\Delta T_{\text{source}}$ is approximately twice larger than that of $\Delta T_{\text{low source}}$. Second, the timing of the interglacial-glacial inception maxima is strongly affected: small $\beta_{\text{site}}$ coefficients induce a maximum $\Delta T_{\text{low source}}$ at the onset of glaciations (MIS 5d), while large $\beta_{\text{site}}$ coefficients place $\Delta T_{\text{source}}$ maxima in phase with Antarctic warmth (MIS 5e). With the exception of glacial inceptions, the new $\Delta T_{\text{source}}$ reconstruction is also much more similar to $\Delta T_{\text{site}}$. Note that a very similar result is obtained by changing only the value of $\beta_{\text{site}}$ from 1.3 (this study) to 0.5 (smaller value) because among four coefficients, only the $\beta_{\text{site}}$ is significantly different from previous estimates. Figure 6a, therefore, shows the fact that the $\beta_{\text{site}}$ coefficient directly affects the glacial-interglacial magnitude of $\Delta T_{\text{source}}$.

In contrast to the sensitivity of $\Delta T_{\text{source}}$ to the uncertainties in regression coefficients, the $\Delta T_{\text{site}}$ shows much less sensitivity (Fig. 6c). Indeed, the difference between $\Delta T_{\text{site}}$ and $\Delta T_{\text{low site}}$ is $\sim 0.6 ^\circ C$, which is within typical error ($10–30 %$) of temperature estimations (Jouzel et al., 2003). Published DF $\Delta T_{\text{site}}$ (which corresponds to $\Delta T_{\text{low site}}$) estimates MIS 9e to be warmer than the present by $4.0 \pm 0.3 ^\circ C$ (Kawamura et al., 2007) (Fig. 6c). Our revised estimate of $4.8 \pm 0.5 ^\circ C$ is slightly warmer than previous MIS 9e $\Delta T_{\text{site}}$ values, but it remains within the uncertainty range. For MIS 5e, previous and our DF $\Delta T_{\text{site}}$ estimates are $3.5 \pm 0.1 ^\circ C$ and $3.7 \pm 0.4 ^\circ C$, respectively. The $\Delta T_{\text{site}}$ records from six Antarctic ice cores also show similar degree of warming during interglacial periods (Masson-Delmotte et al., 2011). A GCM study, based on increased CO$_2$ projections, however, suggested that MIS 5e isotope temperature may have been 6 to 10 $^\circ C$ warmer than present day (Sime et al., 2009). This estimate is significantly larger than any of our reconstructions. Thus, these results suggest that moisture source effects cannot explain the model-data discrepancy.

### 4.2 Comparison with the other cores

The methodology used to obtain $\Delta T_{\text{site}}$ and $\Delta T_{\text{source}}$ at DF is also used on Vostok and EDC data (Table 1). Figure 7 shows the $\Delta T_{\text{source}}, \Delta T_{\text{site}}$, and the temperature gradient records.

The glacial–interglacial changes in $\Delta T_{\text{source}}$ are significantly larger than the estimates using previous MCIM tuning. For Vostok, the new $\Delta T_{\text{source}}$ decreases to about $-6.0 \pm 0.1 ^\circ C$ around 19 kyr BP (temperatures are based on the 1kyr average $\pm 1\sigma$), which is cooler than previous estimates of $\sim -4 ^\circ C$ (Vimeux et al., 2002). For the EDC, the $\Delta T_{\text{source}}$ decrease to $-8.1 \pm 0.3 ^\circ C$ at 19 kyr BP, which is much lower than the previous estimation of $-3$ to $-4 ^\circ C$ (Stenni et al., 2010). This large EDC $\Delta T_{\text{source}}$ variation results from $\beta_{\text{site}}$ value, which results in a larger proportion of $\delta D$ added to the raw $\delta$ record.

The glacial–interglacial changes in $\Delta T_{\text{site}}$ are close to the previous estimations. The Vostok $\Delta T_{\text{site}}$ estimations based on this study decreased to about $-7.1 ^\circ C$ at 19 kyr BP and reached the minimum at $-7.8 ^\circ C$ at 21.7 kyr BP. These values are almost the same as the previous estimates (Vimeux et al., 2002). For the EDC, our $\Delta T_{\text{site}}$ estimate decreases to about $-9.9 \pm 0.2 ^\circ C$ at 19 kyr BP, slightly lower than the previous estimate of $-8$ to $-9 ^\circ C$ at 20 kyr BP without accounting for elevation corrections (Stenni et al., 2003, 2010). The lower $\Delta T_{\text{site}}$ results from combination of relatively larger variation in $\delta D$ and larger $\gamma_{\text{site}}$ values. In summary, as for DF case, the new $\Delta T_{\text{site}}$ estimations of Vostok and EDC cores are consistent with the previous estimates within typical error ($10–30 %$) (Jouzel et al., 2003). Interestingly, at glacial inceptions, all the $\Delta T_{\text{site}}$ records show warmer values than classical $\delta D$-temperature estimates, and thus the co-variation
of $\Delta T_{\text{site}}$ and CO$_2$ found in Vostok core (Cuffey and Vimeux, 2001) is generally supported.

Our reconstructed $\Delta T_{\text{site}}$ and $\Delta T_{\text{source}}$ are lower at EDC than other east Antarctic stations (Fig. 7). This is consistent with a larger $\delta D$ depletion at EDC. A GCM simulation suggests that differences in $\delta$ can be explained primarily by variations in the palaeothermometer gradient (i.e. $\partial \delta / \partial T$), rather than in temperature (Sime et al., 2009). Note that their study does not include correction for moisture source, but used either $\delta D$ or $\delta^{18}$O value. Our study revealed that the moisture source correction based on $d$ value does not explain the isotopic differences, because our $\Delta T_{\text{site}}$ estimate at EDC is still colder than the others.

The temperature gradients ($\Delta T_{\text{source}} - \Delta T_{\text{site}}$) of DF, EDC and Vostok show a strong 40-kyr cycle (Fig. 7). Such marked 40-kyr periodicity has not been found in previous reconstructions of temperature gradient at Vostok (Vimeux et al., 2002) and EDC (Stenni et al., 2010) as the gradient was strongly correlated with $\Delta T_{\text{site}}$ ($r^2 = 0.9$) (Stenni et al., 2010). The glacial–interglacial variations of the gradient of this study ranges from $-2$ to $4 \degree C$. These variations are smaller than the previous by $\sim 2$ to $3 \degree C$ ($\sim 40\%$ smaller). The amplitude of temperature gradient ranged from $-3$ to $6 \degree C$ at Vostok (Vimeux et al., 2002), and $-2$ to $6 \degree C$ at EDC (Stenni et al., 2010).

4.3 Comparison with SST records from ocean sediments

Which (low versus high coefficient) approach is most consistent with independent information? Here, we use sea surface temperature (SST) estimates obtained from ocean proxy records, and compare these to our reconstructed $\Delta T_{\text{source}}$. We are aware that different marine proxies can lead to significant uncertainties in reconstructions, which can also have seasonal biases (e.g. MARGO project members, 2009). The recent synthesis of LGM SST data depicts a latitudinal temperature gradient in the Southern Hemisphere oceans. Backward trajectory models suggest that the present-day main moisture source for DF is located around the 40–70$\degree S$ ocean (Reijmer et al., 2002; Sodemann and Stohl, 2009). In the 42.5–52.5$\degree S$ latitudinal band, the LGM minus present-day anomaly is $-3.8 \degree C$ (MARGO Project Members, 2009). Figure 6b shows a stacked Southern Ocean mid-latitude SST record (Barrows et al., 2007) that was made by combining the ocean sediment records from the MD97-2120 (45$\degree 32\prime$S, 174$\degree 56\prime$E) from east of New Zealand (Pahnke and Sachs, 2006) and MD88-770 (46$\degree 01\prime$S, 96$\degree 27\prime$E) from the Indian Ocean (Labeyrie et al., 1996). The stacked SST record shows a relatively large SST shift ($\sim 5 \degree C$) during Termination I. Another sediment core (MD07-3076) retrieved in the Atlantic sector of the Southern Ocean (44$\degree 09\prime$S, 14$\degree 13\prime$W) shows a glacial–interglacial temperature change of $\sim 7 \degree C$ both during Termination I (Skinner et al., 2010) and Termination V (Vázquez Riveiros et al., 2010).

Our $\Delta T_{\text{source}}$ variation based on isotope-fitting is therefore only compatible with the largest SST amplitude estimates. However, the moisture source likely moves between glacial and interglacial periods, as suggested by water tagging in atmospheric models (Delaygue et al., 2000) or abrupt shifts of $d$ (Masson-Delmotte et al., 2010a). During glacial periods, northward shifts of the mean evaporation locations are expected to compensate the impact of SST cooling into $\Delta T_{\text{source}}$. While associated with uncertainties on the actual moisture sources and the proxy-based SST reconstructions, this comparison suggests that our large $\Delta T_{\text{source}}$ reconstruction is at the upper limit of compatibility with SST data. Note that the $\Delta T_{\text{source}}$ estimated using MCIM indicates ocean surface temperature averaged (vapor amount weighted) by different moisture sources. Thus, separating the source-areas requires additional information (i.e. chemical composition, backward trajectory analysis, and general circulation model, etc.). There are also several limitations for the $\Delta T_{\text{source}}$ reconstruction caused by uncertainties on supersaturation and precipitation intermittency in different past climate conditions.

4.4 Obliquity and deuterium-excess

A strong 41-kyr Earth’s obliquity periodicity is detected in many paleoclimatic SST records, in both hemispheres (Corr¡jo et al., 1999; Sachs et al., 2001) including ice cores (Jouzel et al., 2007). Based on this paleoclimatic evidence, obliquity was suggested to be a key driver of glacial–interglacial dynamics (Vimeux et al., 1999, 2001; Khodri et al., 2001; Raymo and Nisancioglu, 2003; Loutre et al., 2004; Huybers and Wunsch, 2005; Lee and Poulsen, 2008; Davis and Brewer, 2009).

The raw $d$ record from Antarctic ice cores also shows a strong 41-kyr obliquity periodicity (Stenni et al., 2001, 2003, 2010; Vimeux et al., 1999; Uemura et al., 2004). Previous studies suggested that the obliquity component of the Vostok $d$ record could be related to the contrasting impact of obliquity on annual mean insolation and temperature at low and high latitudes (affecting SST), amplified by changes in the moisture transport induced by the annual insolation gradient between low and high latitudes (Vimeux et al., 1999; Loutre et al., 2004). In previous reconstructions, $\Delta T_{\text{source}}$ was similar to the raw deuterium excess signals and showed a large obliquity imprint.

Interestingly, $\delta D$ and $d$ are anti-correlated in the 40-kyr band (Fig. 8). As a result, small differences in $\beta_{\text{site}}$ have large impacts on the obliquity signal in $\Delta T_{\text{source}}$. Spectral analysis shows that our new $\Delta T_{\text{source}}$ reconstruction indeed has a weak obliquity signal (Fig. 9). It cannot therefore be ruled out that the strong obliquity signal found in the raw $d$ records of DF and Vostok cores is an artifact of site temperature. This does not apply to EDC where the obliquity imprint in the raw $d$ is less clear.
is an antiphase of obliquity) is $1.3 \pm 0.4$ kyr. The gradients of EDC and Vostok also lag the obliquity by $1.9 \pm 0.7$ and $0.9 \pm 0.5$ kyr, respectively. This differs from the observed 5 kyr lag between EDC $\delta^1T$ and obliquity (Jouzel et al., 2007). The processes responsible for the observed lags remain elusive, and likely involved the interplay between ice sheets and ocean circulation. Further investigations of the mechanisms linking obliquity and site-source temperature gradient are required, in order to use such information for orbital dating of ice cores. It will provide independent evidence to test the length of MIS 11, in which the accuracy of the EDC3 age scale (Parrenin et al., 2007) was questioned (Masson-Delmotte et al., 2010b; Pol et al., 2011).

### 5 Conclusions and perspective

We obtained a new $d$ record from DF ice core spanning the past 360 000 yr and compared this with records from Vostok and EDC ice cores. To interpret the $d$ and $\delta^1D$ records as $\Delta T_{\text{source}}$ and $\Delta T_{\text{site}}$ information, we used an isotopic inversion methodology based on the MCIM model as previously performed by Vimeux et al. (2002); Stenni et al. (2001) on the Vostok and EDC ice cores respectively. A major source of uncertainty lies in the coefficient of regression, $\beta_{\text{site}}$ which is related to the sensitivity of $d$ to $\Delta T_{\text{site}}$. We showed that different ranges of temperature and selections of isotopic model outputs increase the value of $\beta_{\text{site}}$ by a factor of two. The results suggests that the differences of $\beta_{\text{site}}$ from previous studies are due to the isotopic model tuning for the present-day, and the $\delta^1D$ ranges selected for regression analyses. We have shown that the $\beta_{\text{site}}$ depends on the range of temperature or isotopic depletion used.

For the first time, we applied the exact same temperature inversion methodology to the three Antarctica ice cores data sets (DF, Vostok, and EDC). All $\Delta T_{\text{source}}$ records were sensitive to the inversion method, with our new approach (isotope-fitting) leading to amplitudes of $\Delta T_{\text{source}}$ variation $\sim 2^\circ C$ to $4^\circ C$ larger compared to the previous estimations. For DF, the $\Delta T_{\text{source}}$ estimates yields values between $-5.9^\circ C$ and $2.9^\circ C$ over the past 360 kyr. Comparisons with proxy-based SST records suggest that our large $\Delta T_{\text{source}}$ reconstruction is at the upper limit of compatibility with SST data. In contrast to the significant modification in $\Delta T_{\text{source}}$, the $\Delta T_{\text{site}}$ records were not modified significantly and therefore appear robust. The differences between the current and previous studies are within published uncertainty ($-10–30\%$) of $\Delta T_{\text{site}}$ estimations. The new $\Delta T_{\text{source}}$ estimates showed only weak 41-kyr obliquity periodicity, but the obliquity signal was found in the temperature gradient ($\Delta T_{\text{source}} - \Delta T_{\text{site}}$). The temperature gradient records of the three cores show a systematic anticorrelation with obliquity, providing new evidence for the importance of the Earth’s obliquity as a driver of water cycle and climate dynamics. Such properties offer the perspective

---

**Fig. 8.** Obliquity components of the DF isotope records. (a) Earth’s obliquity, (b) the raw $d$ record of DF (black dotted line) and its filtered signal (red solid line). The filtered obliquity component was obtained by Gaussian filters with the Analyseries program (Pallard et al., 1996). A band-pass filter in the obliquity band ($f \approx 0.025 \pm 0.005$) was calculated (red solid line). (c) Filtered components in the DF $d$ (red solid line) and $\delta^1D$ (black solid line). (d) the $\delta^1D$ (black dotted line) record of DF and its filtered signal (black solid line).

As a result of our new reconstruction, spectral properties of our temperature gradient ($\Delta T_{\text{source}} - \Delta T_{\text{site}}$) from DF, Vostok and EDC cores appears mainly modulated by obliquity (Fig. 9) and without 100 kyr cycles. A recent modeling study (Anticco et al., 2010) supports a large control of obliquity on latitudinal moisture transport.

Compared with $\delta^1D$, the strong imprint of obliquity is reduced in our $\Delta T_{\text{site}}$ reconstruction (Fig. 9), suggesting that it can be partly affected by moisture origin effects. The obliquity signal, however, remains in $\Delta T_{\text{site}}$. Thus, the moisture source effect cannot fully explain the fact that climate models display a negligible impact of obliquity on the simulated annual mean Antarctic temperature, suggesting that it may result from model biases, such as a lack of austral sea ice in control simulations (Masson-Delmotte et al., 2010b).

Furthermore, our synchronized age scale is based on the imprint of precession on DF O$_2$/N$_2$ and is independent from orbital properties of the stable isotope records. In our high $\beta_{\text{site}}$ case, the site-source temperature gradient mainly exhibits obliquity periodicities, which is a requested characteristic for orbital tuning. Cross spectrum analysis shows that the mean lag of this reconstructed temperature gradient behind the annual mean insolation gradient (Fig. 7c; which
Fig. 9. Power spectra of DF core isotope records. Power spectra of DF (red), Vostok (blue), and EDC (green): (a) δD, (b) d, (c) Ocean isotope change (δ^{18}O_{sw}) over the past 360 kyr (Bintanja and Wal, 2008), (d) ΔT_{site}, (e) ΔT_{source}, and (f) temperature gradient (ΔT_{source} − ΔT_{site}). Spectral analysis is performed using Blackman-Tukey analysis with 50% of series lag (for DF, Vostok, and δ^{18}O_{sw}) and 70% (for EDC) with the Analyseries software (Paillard et al., 1996).

of using this obliquity imprint as a synchronization tool for dating ice cores.

The isotope inversion method involves simplification, and the procedure is challenging, in particular in Antarctica where isotope ratios are extremely depleted. Analyzing d at an event basis in modern condensing vapor and precipitation is useful when combined with moisture tracking analysis (Sodemann and Stohl, 2009) and isotopic modeling, to identify hypotheses and parameterizations in distillation models regarding the controls of d. Our results depend on the prescribed fractionation coefficients. It is also necessarily to improve the quantification of isotopic fractionation coefficients of under kinetic condition (Luz et al., 2009; Uemura et al., 2010b) and equilibrium condition at very low temperatures (Ellehoj et al., 2012). Triple isotope ratios of oxygen (i.e. ^{17}O-excess) in water molecules (Landais et al., 2008, 2011; Luz and Barkan, 2010; Winkler et al., 2012) would also provide independent evidence for moisture source imprint on isotopically depleted snow. Finally, extensive field observation of d and ^{17}O-excess in clouds over Antarctica may provide better constraints on supersaturation function, and will allow to improve our understanding of the mechanism underlying the changes in d and ^{17}O excess.

Appendix A

Logarithmic definition of d and meaning of β_{site}

The interplay of artifacts caused by the empirical d definition and by physical kinetic processes (evaporation and snow formation) restricts precise physical understanding of meaning to the value of two coefficients (β_{site} and β_{source}) in Eq. (4). The empirical definition (i.e. the constant slope of 8) of d itself induces changes in d because any process that does not follow the δD/δ^{18}O slope of 8 alters the d value. Indeed the δD/δ^{18}O slope can deviate from the mean value of 8 because of the combination of the nonlinearity of the ratio of equilibrium-fractionation factors and the crude approximation of ln(1+δ) ∼ δ. In contrast to the historical linear definition of d, recent studies of triple oxygen isotope study of water have used the logarithmic framework for defining the ^{17}O-excess parameter (Barkan and Luz, 2007). Here, we examine how the historical definition of d affects the ice core d record and β_{site} by introducing a logarithmic based definition of deuterium excess.

In the normal δ plot, the slope of Global Meteoric Water Line (GMWL) apparently keeps a constant value “8” along
GMWL data based on 308 stations whose data contains the \( d \) data longer than 2 yr. The GNIP data weighted by amount of precipitation give a recession line (\( \delta D = 8.18 \times \delta^{18}O + 11.2 \) \( (R^2 = 0.999) \)). (b) Same as (a) but plot on the log plot. All the data give a regression curve (GMWC): \( \ln(1 + \delta D) = -2.85 \times 10^{-2} \times (\ln (1 + \delta^{18}O))^2 + 8.47 \times \ln (1 + \delta^{18}O) + 13.3 \) \( (R^2 = 0.999) \).

Unlike a constant slope of GMWL, the slope of this Global Meteoric Water Curve (GMWC) increases from \( \sim 8.5 \) to 12 as \( \ln(1 + \delta^{18}O) \) decreases. Figure A2 shows the slope and \( \ln(1 + \delta^{18}O) \) with corresponding annual-mean surface air temperature. This slope generally agrees with the one expected from \( (\alpha_D - 1)/(\alpha_{18^O} - 1) \). There is a clear gap between the transition of equilibrium fractionation factors for liquid-vapor and ice-vapor for \( ^{18}O \) (Majoube, 1971a, b) and for D (Merlivat and Nief, 1967). The gap was narrowed after incorporating the super saturation effect (Jouzel and Merlivat, 1984) (here, we used the \( S_i \) function described in Sect. 2.2. was used).
Based on the GMWC, a deuterium-excess paramter based on logarithmic $\delta$, hereafter denoted as $d_{\text{ln}}$, is defined as

$$
d_{\text{ln}} = \ln(1 + \delta D) - (-2.85 \times 10^{-2} \times (\ln(1 + \delta^{18}O))^2 + 8.47 \times \ln(1 + \delta^{18}O)). \quad (A2)
$$

In contrast to the $d$, which shows parabolic curve against $\delta^{18}O$, $d_{\text{ln}}$ does not depend on $\ln(1 + \delta^{18}O)$ (Fig. A1b). Note that $d_{\text{ln}}$ is defined based on phenomenological data set. Thus, not only the equilibrium effect but also kinetic fractionation (like snow formation effect) is also eliminated.

Figure A3 shows the $d_{\text{ln}}$ records of Antarctic ice cores. The $d_{\text{ln}}$ ranges from about $-15$ to $5 \% e$. The glacial–interglacial amplitude is, thus, about two times larger than the normal $d$ variation. Unlike raw $d$ records, the $d_{\text{ln}}$ records does not shows distinct $~40 \text{ kyr}$ cycle nor the lag found in the glacial terminations. These results show that glacial–interglacial variations of $d$ record are sensitive to its definition. Thus, great care should be taken to interpret such second-order parameter.

With the same methodology used for the $d$, the $d_{\text{ln}}$ data can be converting to the $\Delta T_{\text{site}}$ and $\Delta T_{\text{source}}$. For the correction for ocean isotope changes, $\ln(1 + \delta)$ gives simpler formula than the case for normal $\delta$.

$$
\ln(1 + \delta^{18}O)_{\text{corr}} = \ln(1 + \delta^{18}O_{\text{ice}}) - \ln(1 + \delta^{18}O_{\text{sw}}) \quad (A3)
$$

$$
\ln(1 + \delta D)_{\text{corr}} = \ln(1 + \delta D_{\text{ice}}) - \ln(1 + \delta D_{\text{sw}}). \quad (A4)
$$

Here, $\ln(1 + \delta^{18}O)_{\text{corr}}$ and $\ln(1 + \delta D)_{\text{corr}}$ are the isotope ratios of the ice corrected for ocean isotope changes. The $\delta D_{\text{sw}}$ can be calculated on the assumption that $\ln(\delta D_{\text{sw}} + 1) = -2.85 \times 10^{-2} \times (\ln(1 + \delta^{18}O_{\text{sw}}))^2 + 8.47 \times \ln(1 + \delta^{18}O_{\text{sw}})$. Thus, the $d_{\text{ln}}$ value corrected for the ocean isotope effect ($d_{\text{ln,corr}}$) can be obtained by substituting $(1 + \delta^{18}O_{\text{corr}}$ and $(1 + \delta D)_{\text{corr}}$ to the Eq. (A2). Then, the isotope inversion was performed to retrieve the $\Delta T_{\text{site}}$ and $\Delta T_{\text{source}}$ information. The relations obtained for the DF ice core are

$$
\Delta \ln(1 + \delta D)_{\text{corr}} = 13.5 \Delta T_{\text{site}} - 5.5 \Delta T_{\text{source}} \\
(R^2 = 0.999, n = 14, p < 0.001) \quad (A5)
$$

$$
\Delta d_{\text{ln,corr}} = -0.4 \Delta T_{\text{site}} + 1.8 \Delta T_{\text{source}} \\
(R^2 = 0.996, n = 14, p < 0.001) \quad (A6)
$$

We should note that we only modified the notation of $\delta$ and the definition of $d$. The two primary data sets ($\delta D$ and $\delta^{18}O$) and inversion methodology are the same. Therefore, the $\Delta T_{\text{site}}$ and $\Delta T_{\text{source}}$ obtained based on the Eqs. (A5) and (A6) are identical with those of obtained based on the Eqs. (5) and (6). The values of coefficients of the Eqs. (A5) and (A6) differ from those of Eqs. (5) and (6). The coefficient $\beta_{\text{site}} (0.4)$ is significantly smaller than our estimation (1.3). This result clearly shows the fact that the value of $\beta_{\text{site}}$ significantly depends on the definition of deuterium excess. In other word, $\beta_{\text{site}}$ act as a correction factor for the empirically defined $d$ parameter. Detailed and comprehensive analysis of $d_{\text{ln}}$ (e.g. other Antarctic sites, Greenland ice cores, and global precipitation) is beyond the scope of this manuscript. At least for the case of DF, the smaller $\beta_{\text{site}}$ value indicates that the $d_{\text{ln}}$ is better representation of source effect. In general, $d_{\text{ln}}$ would be suitable for comparison with similarly defined parameter, $\delta^{17}O$-excess.

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